



#### Heat Transfer Theory

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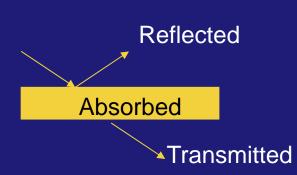
#### Modes of heat transfer

- Law of physics
  - Heat = Energy
  - If you take a hot spot
  - ... and a cold spot
  - ... the heat will **always** be transferred from the hot to the cold

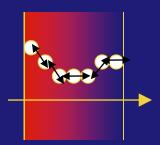


### Three ways to transfer heat

- Radiation
  - Electromagnetic waves
  - When it reaches a body it has 3 options:

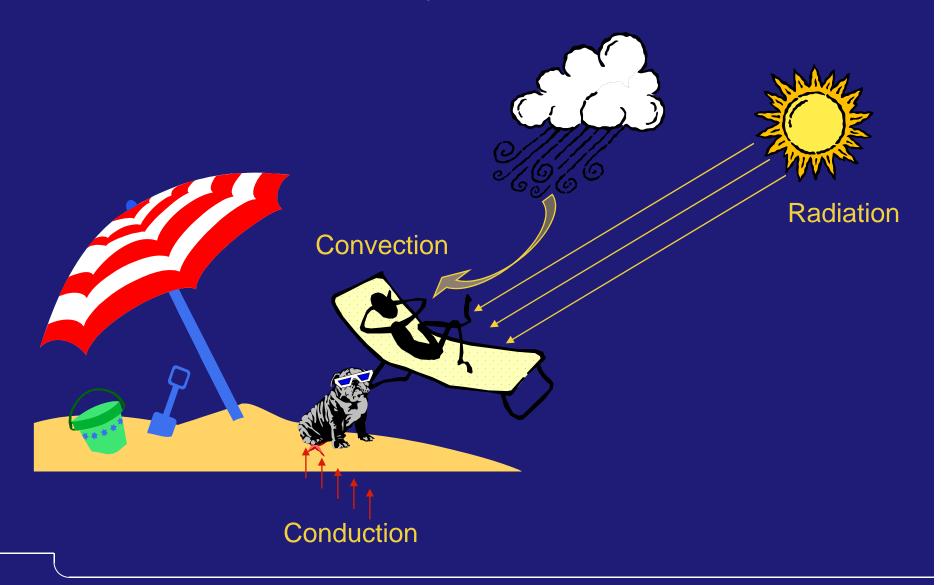


- Conduction
  - Molecular or atomic vibrations
  - No material transport



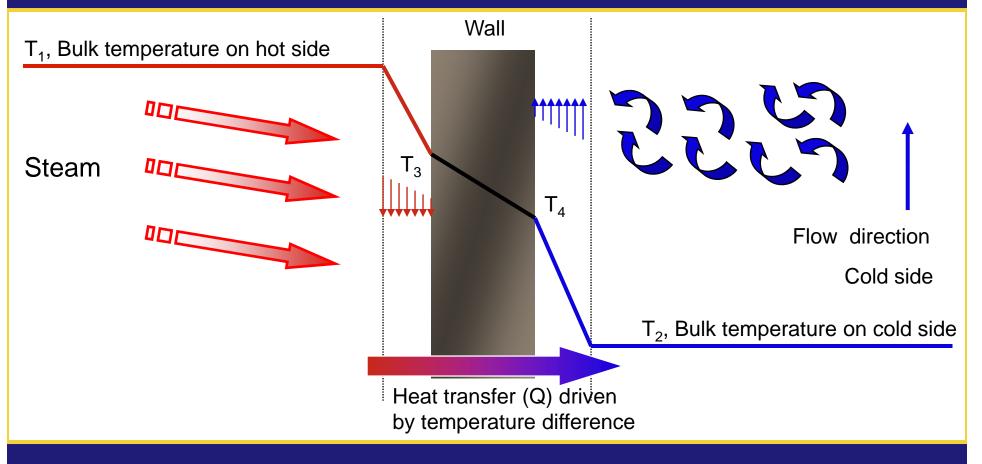
- Convection
  - Energy is transferred by the motion and intermixing of small mass elements
  - Natural convection caused by density difference
  - Forced convection is man-made (ex., pump)

# Example, a day at the beach



#### Heat Transferred in a HE

The temperature profile at one point of the plate wall



## The Heat Transfer Equation

## The Heat Transfer equation

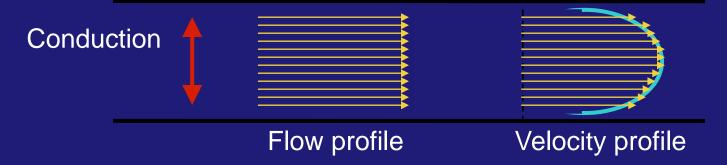
$$Q = k * A * LMTD$$

- Q = Heat Load, W (same as  $Q_1 = Q_2$  before)
- k = k-value, overall heat transfer coefficient (OHTC), W/m<sup>2</sup>°C
  - Higher k-value = More efficient heat transfer
- A = heat transfer area (m²)
- LMTD= Logarithmic mean temperature difference

## The Heat Transfer Equation

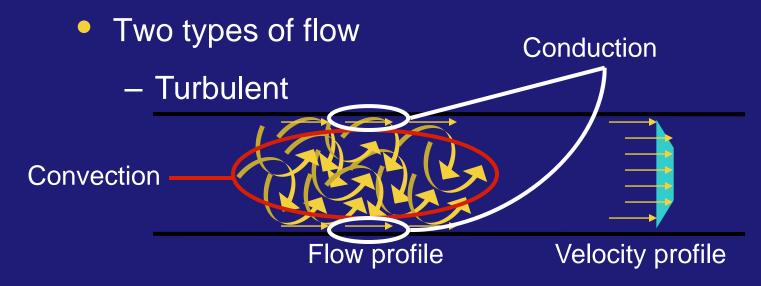
## Flow principles

- Two types of flow
  - Laminar



- Orderly flow throughout the fluid
- Parabolic flow profile
  - Fluid at the wall moves slower
  - Due to the friction from the wall surface
- Ex., viscous fluids or water at low velocity

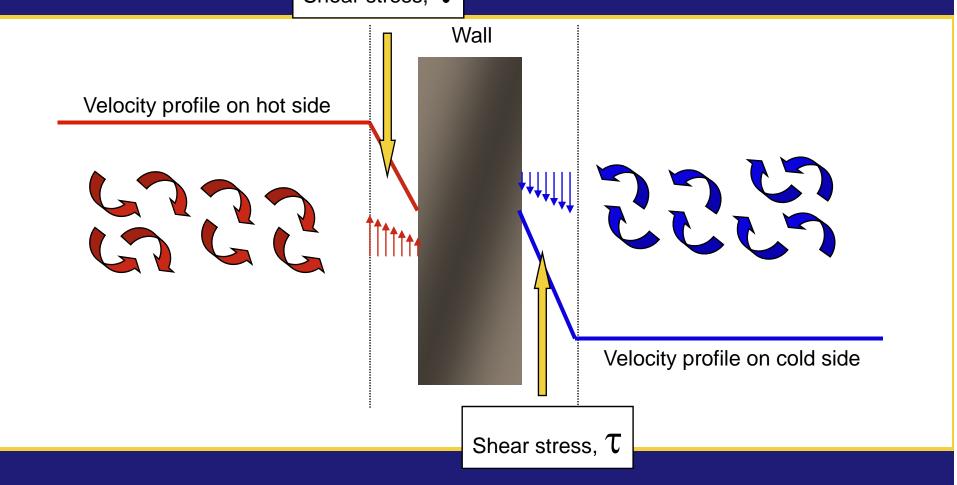
## Flow principles



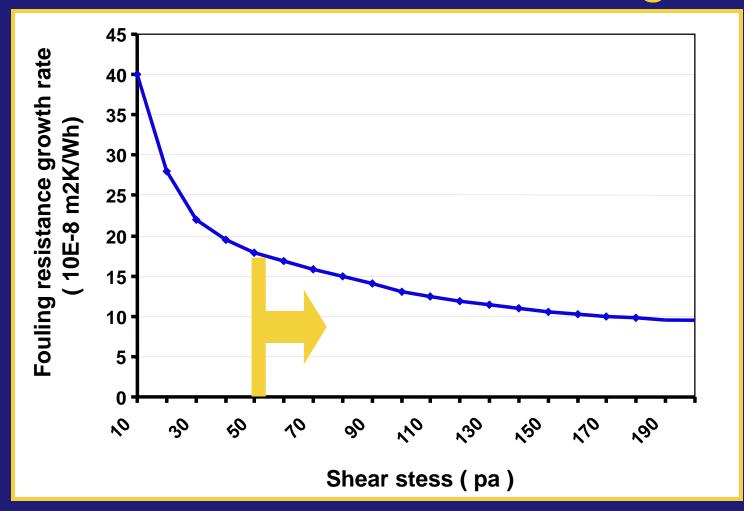
- No orderly flow
- Random eddy motion mixes the fluid
- Always a laminar film closest to the wall
- Ex., water at higher velocity

#### **Shear Stress**

Shear stress,  $\boldsymbol{\tau}$ 

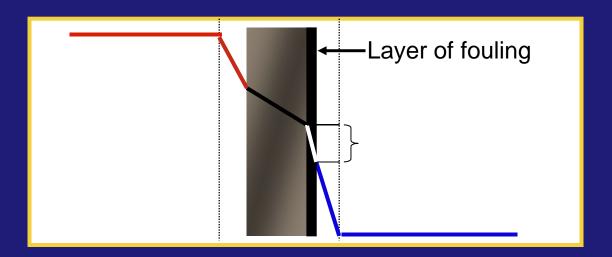


#### Shear stress versus fouling rate



Rule of thumb: Try to keep the shear stress >50 Pa

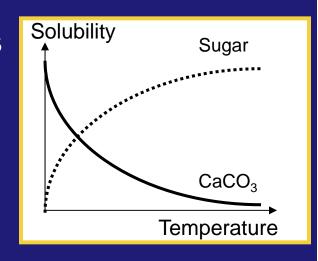
# Fouling



- Major debris
- Biological growth
- Scaling
- Sedimentation
- Burn-on

# Scaling

- Reversed solubility of dissolved salts
  - Reduced solubility at higher temperature
  - Ex CaCO<sub>3</sub> and Ca(PO<sub>4</sub>)<sub>2</sub>
- Common problem
  - Keep wall temperature low
  - Design with high shear stress  $(\tau)$



## Design Safety Factors

- k-value margin (for PHEs)
  - Defined as a % margin between k<sub>Clean</sub> and k<sub>Service</sub>

$$Margin = \frac{k_{clean} - k_{service}}{k_{service}} (\%)$$

$$Margin = \frac{A_{act} - A_{req}}{A_{req}} (\%)$$

## S&T use Rf – the Fouling Factor

- Normal Rf for S&T:  $1.0 \times 10^{-4}$  m<sup>20</sup>C/W

 $5.0 \times 10^{-4}$  ft<sup>2.0</sup>F,h/Btu

Normal k<sub>Clean</sub> for PHE: 6000
 W/ m<sup>20</sup>C

1000 Btu/ft<sup>2,o</sup>F,h

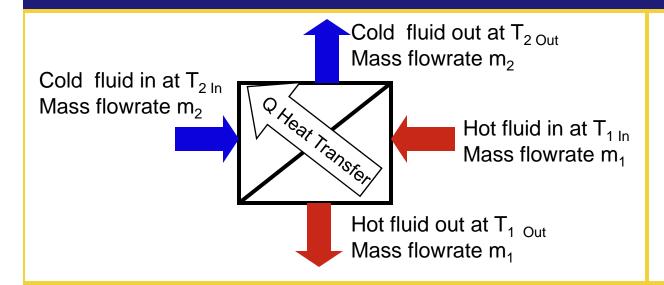
$$\frac{1}{k_{\text{Service}}} = \frac{1}{k_{\text{Clean}}} + R_f = \frac{1}{6000} + 10^{-4} \implies k_{\text{Service}} = 3750 \text{ W/ m}^{2} \text{°C}$$

Corresponding k-value margin

$$M \arg in = 100 \cdot \frac{k_{clean} - k_{service}}{k_{service}} = 100 \cdot \frac{6000 - 3750}{3750} = 60\%$$

- Much too high margin
  - Too many plates ⇒ Less turbulence ⇒ Fouling!
  - Maybe not competitive?

Liquid-to-liquid



#### **Definitions**

Q = Heat load, W (rate of heat transfer)

m = Mass flow rate, kg/s

Cp= Specific heat, J/kg°C (the energy needed to heat 1 kg of the fluid with 1°C)

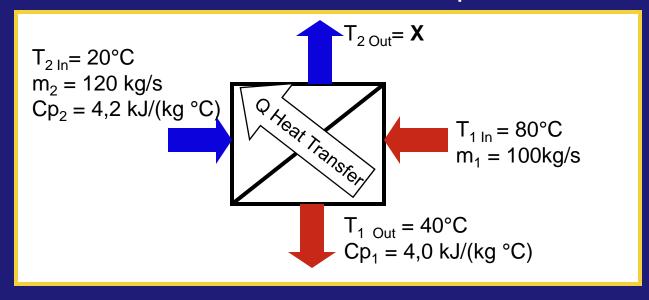
Heat released by the hot fluid:  $Q_1=m_1*Cp_1*(T_1 ln-T_1 Out)$ 

Heat absorbed by the cold fluid:  $Q_2=m_2*Cp_2*(T_2out-T_2ln)$ 

Heat losses are negligible  $\Rightarrow$  Q<sub>1</sub>= Q<sub>2</sub>

#### The Heat Balance - calculation

What is the cold fluid outlet temperature?



Heat Load:  $Q_1 = m_1 * Cp_1 * (T_{1 \text{ In}} - T_{1 \text{ Out}}) = 100 \text{ kg/s} * 4.0 \text{ kJ/(kg °C)} * (80-40) °C$ 

$$Q_1 = 16\ 000\ kJ/s = 16\ 000\ kW$$

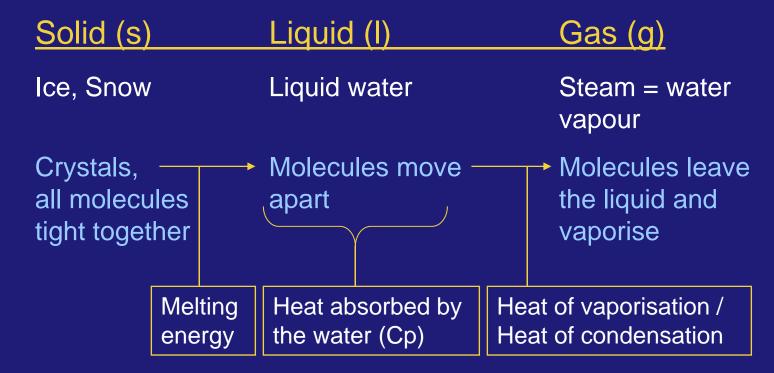
$$Q_1 = Q_2$$
: 16 000 kW =  $Q_2 = m_2 * Cp_2 * (T_2 Out - T_2 In)$ 

$$16\ 000\ kW = 120\ kg/s * 4.2\ kJ/(kg °C) * (X-20)°C$$

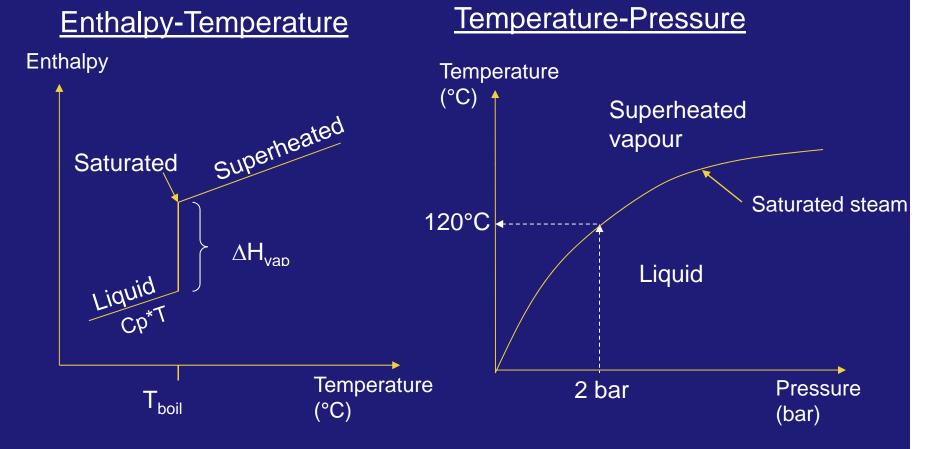
Steam-to-liquid

Everyone knows what steam is?

- The three three phases of water:



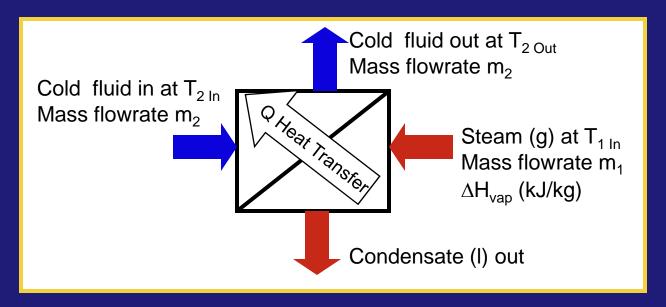
Steam described in diagrams



 $\Delta H_{\text{vap}}$  = Heat needed to vaporise 1 kg of a fluid (kJ/kg)

The same amount of energy is released during condensation

Steam-to-liquid



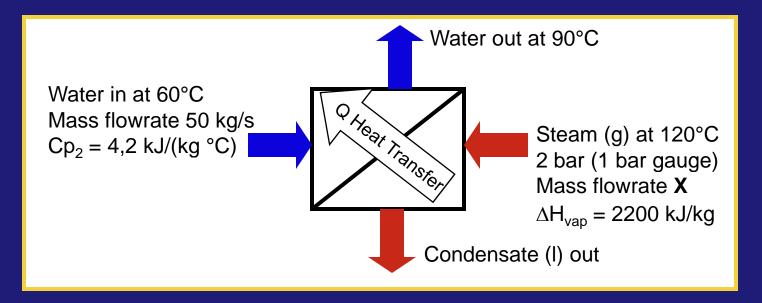
Heat released by the steam:  $Q_1=m_1^* \Delta H_{vap}$ 

Heat absorbed by the cold fluid:  $Q_2=m_2*Cp_2*(T_2out-T_2ln)$ 

Heat losses are negligible  $\Rightarrow$  Q<sub>1</sub>= Q<sub>2</sub>

#### The Heat Balance - calculation

How much steam is needed to heat the water?



Heat Load:  $Q_2 = m_2 * Cp_2 * (T_{2 \text{ Out}} - T_{2 \text{ In}}) = 50 \text{ kg/s} * 4.2 \text{ kJ/(kg °C)}$  (90-60)°C

$$Q_2 = 6 300 \text{ kW}$$

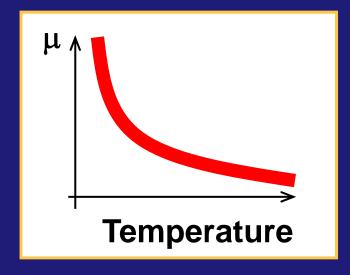
$$Q_2 = Q_1$$
: 6300 kW =  $Q_1 = m_1^* \Delta H_{vap}$   
 $= \frac{6300 \text{ kW} = X \text{ kg/s} * 2200 \text{ kJ/kg}}{2}$ 

. . . . . . . .

- So why is steam used?
  - Less than 3 kg steam can heat 50 kg water from 90 to 60°C
  - It is a high-energy carrier!
- Steam is the most common way in industry to distribute energy for heating purposes

## Physical properties

- Density (ρ)
- Specific heat (Cp)
- Thermal conductivity (λ)
- Viscosity (μ)



Small variations
One value acceptable

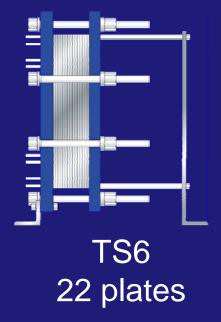
Three values!

## Example phys prop

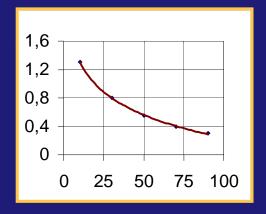
Heating of water 60 to 80°C, 500 kW, steam 2 bar(a)

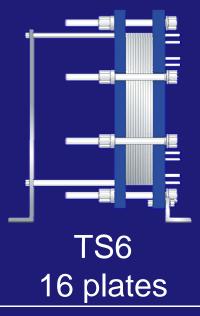
1. Constant viscosity

$$\mu = 1 \text{ cP}$$



#### 2. True viscosity



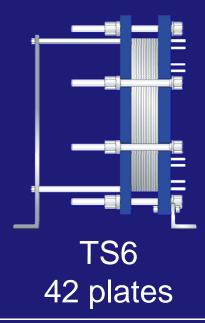


### Example phys prop

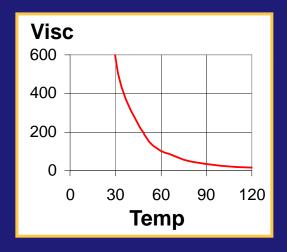
Heating of HFO 30 to 120°C, 400 kW, steam 6 bar(a)

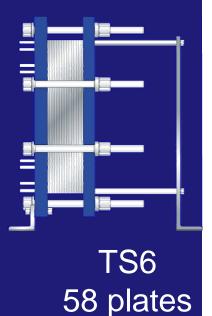
#### 1. Constant viscosity

$$\mu = 10 \text{ cP}$$



#### 2. True viscosity





#### Conventional PHE vs Steam PHE

Heating of water 60 to 80°C, 500 kW, steam 2 bar (a)

#### **M10M**



#### TS6M



Area: 2,6 m<sup>2</sup>

Margin: 25%

P-drop: 45 kPa

Area: 1,9 m<sup>2</sup>

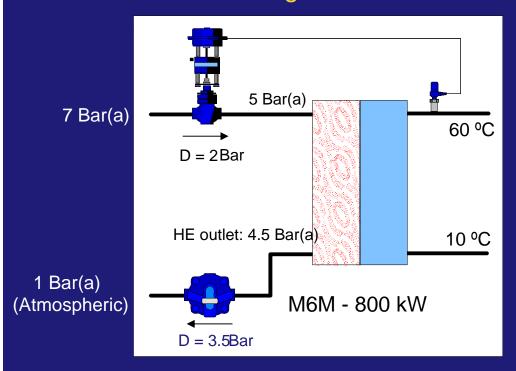
Margin: 6%

P-drop: 35 kPa

# Sizing HE's correctly...

If you ignore the margin.....

Margin = 72 %



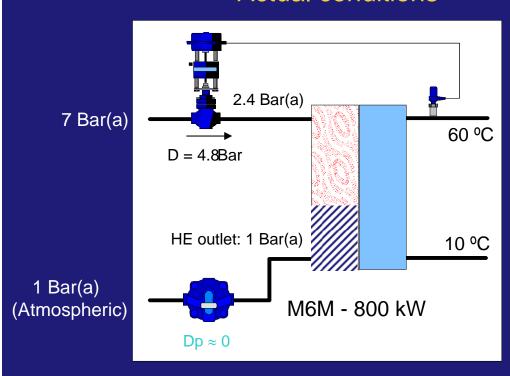
Example of sizing a HE for condensing at 5 Bar(a)

Result: M6M, surface = 1,7 m<sup>2</sup>, margin = 72 %

## Sizing HE's correctly...

#### You could get serious problems!

#### **Actual conditions**



Typical margin related problems are:

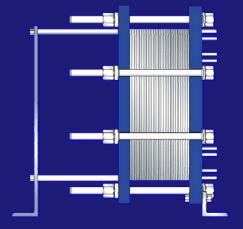
- Over sized control valve
- Under sized steam trap
- Stalled heat exchanger
- High steam velocities

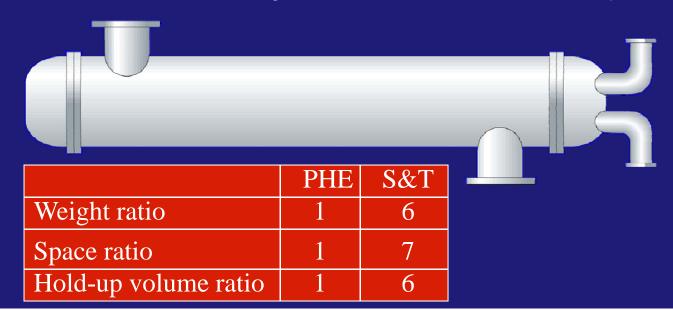
#### PHE versus S&T in steam applications

- Size and weight
- Fatigue
- Thermal efficiency
- Condensation temperature
- Subcooling of condensate
- Temperature control
- Operation in stall condition

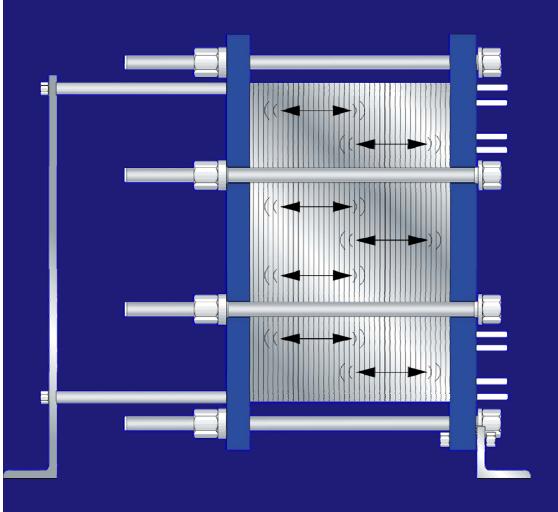
## Size and weight

- PHE requires less floor area
- PHE weighs less
- Easy installation
- Low PxV
  - For small heat exchangers pressure vessel certificates and regular inspection are unnecessary





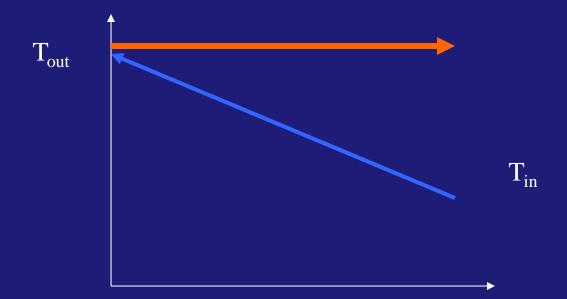
# Fatigue



 Thanks to the elasticity of the gaskets, there will be no thermal fatigue problems in the PHE plate pack

## Thermal efficiency

- A close temperature approach is possible in a PHE
- PHE higher k-value



## A lower condensation temperature

#### Condensation at 150 °C

Load: 1 MW, 60 - 80 °C

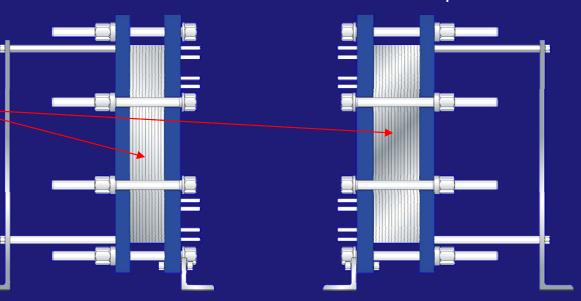
TS6-M with 20 plates

Very small difference in no of plates

#### Condensation at 120 °C

Load: 1 MW, 60 - 80 °C

TS6-M with 28 plates

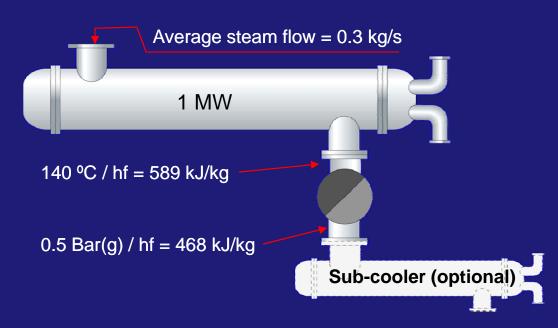


Why design with a low condensation temperature?

- Minimise flash steam
- Reduce scaling
- No pressure build up in the condensate system

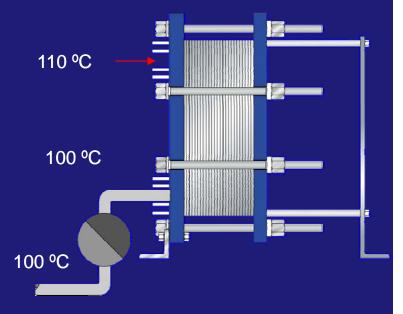
### PHE provides minimum of flash steam

Max condensation temp. 160 °C Average condensation temp. 140 °C



Average operation time; 6,000 hr/year Energy cost; 25 Euro / MWh

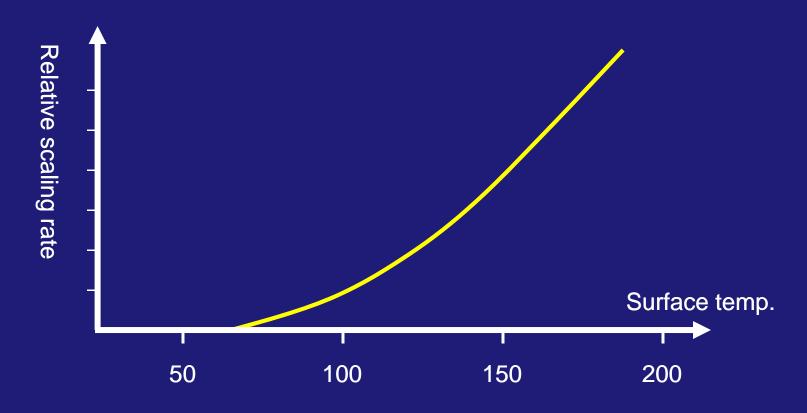
Q = m\*(hfin-hfout)\*time = 0.3\*(589-486)\*6,000 = 185,400 kWh Energy cost = 25\* 185.4 = 4635 EURO / Year Max condensation temp. 120 °C Average condensation temp. 110 °C



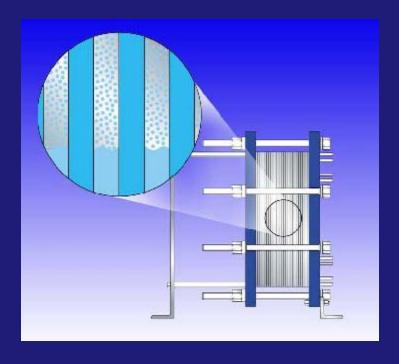
- No losses
- Minimum scaling
- No need to sub cool the condensate
- No pressure build up in the condensate system

## Benefits compared to S&T

Minimised condensation temperature reduce scaling

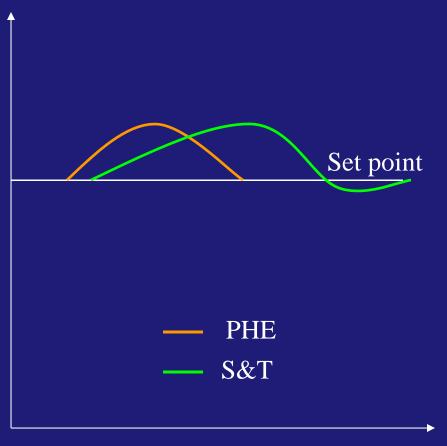


## Subcooling of condensate



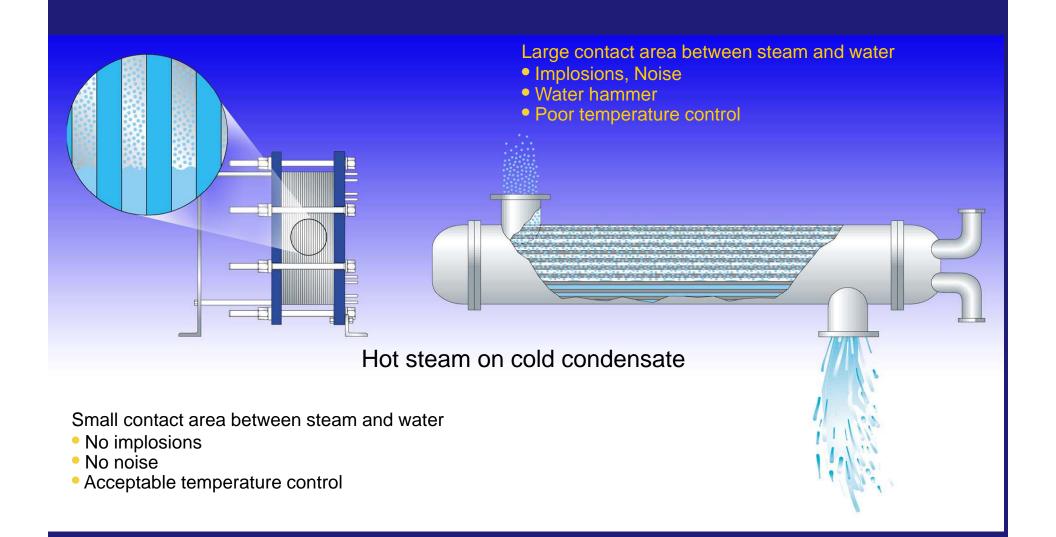
- Possibility of introducing condensate level control and utilising the lower part as a subcooler
- Vertical orientation of the plates makes drainage easy in a PHE

### Temperature control accuracy



 Low hold-up volume, high thermal efficiency and low weight provides a short response time and an accurate temperature control

#### PHE can handle stall conditions



## Summary PHE versus S&T

- PHE compact and easily extendable
- Temperature control accuracy
  - PHE short response time
- Low condensation temperature minimises scaling and flash steam
- PxV

